

Polynomials Card Sort

$f(x) = 2x^3 - x^2 - 7x + 6$	$2x^3 + ax^2 + bx + 6$ $(x - 1)$ is a factor and the remainder on dividing by $(x + 1)$ is 10.
$(1,0), (3,30), (5,196)$	Roots $-2, 1, \frac{3}{2}$
$y - \text{intercept} = (0,6)$	$(2x - 3)(x + 2)(x - 1)$
$f(x) = 2x^3 + 9x^2 + 13x + 6$	All negative roots
$y - \text{intercept} =$	$\frac{2x^4 + 5x^3 - 5x^2 - 20x - 12}{x - 2}$
$(x + 1)$ is a factor	$ax^3 + bx^2 + cx + 6$ Remainder on division by $(x - 2), (x - 1), (2x - 1)$ are 84, 30 and 15 resp.

$$(x + 2)(2x^2 + 5x + 3)$$

$$\frac{2x^4 + 3x^3 - 9x^2 - 8x + 12}{x + 2}$$

$$(2x^2 + x - 6)(x - 1)$$

$$(2x^3 + 6x^2 - 8) - (7x^2 + 7x - 14)$$

$$\sum \alpha = \frac{1}{2}$$

$$\sum \alpha\beta = -\frac{7}{2}$$

$$\sum \alpha\beta\gamma = -3$$

$$\sum \alpha = -\frac{9}{2}$$

$$\sum \alpha\beta = \frac{13}{2}$$

$$\sum \alpha\beta\gamma = -3$$

Let α, β and γ be the roots of $8x^3 - 2x^2 - 7x + 3$. Find the polynomial with roots
 $2\alpha, 2\beta, 2\gamma$

$$\alpha^2 + \beta^2 + \gamma^2 = \frac{29}{4}$$

$$\sum \alpha^2\beta = -\frac{81}{4}$$

Let α, β and γ be the roots of $2x^3 + 3x^2 + x$. Find the polynomial with roots $\alpha - 1$, $\beta - 1$ and $\gamma - 1$

$$f(x) = x^2 + 4x + 4$$

$$\begin{aligned}\alpha + \beta &= -4 \\ \alpha\beta &= 3\end{aligned}$$

Let α and β be the roots of $x^2 + 8x + 12$. Find the polynomial with roots $\frac{\alpha}{2}$ and $\frac{\beta}{2}$.

$$f(4) = 35$$

$$2x^2 + 10x + 6$$

$$\begin{aligned}\alpha + \beta &= -5 \\ \alpha\beta &= 3\end{aligned}$$

$$\alpha^3 + \beta^3 = -80$$

$$\frac{1}{\alpha} + \frac{1}{\beta} = -\frac{5}{3}$$

$$f(x) = 2x^2 - 3x - 20$$

$$(2x + 5)(x - 4)$$

Roots $x = 4$ and $x = -\frac{5}{2}$

$$\begin{aligned}\alpha + \beta &= \frac{3}{2} \\ \alpha\beta &= -10\end{aligned}$$

$$\alpha^2 + \beta^2 = \frac{89}{4}$$

Let p and q be the roots of $18x^2 - 9x - 20 = 0$. Find the quadratic with roots $3p$ and $3q$.