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Show that
$$\int -\frac{1}{\sqrt{1-x^2}} dx = \arccos(x) + C$$
by
using the substitution $x = \cos(u)$.

Prove that $x = n^3 - n$ is divisible by 12
for all odd integers $n > 2$.

Sketch $y = \frac{3}{x}$ and $y = \frac{4}{x^2}$ on the same
graph and state the equation of the
asymptotes.

The points A and B have coordinates
(1,6) and (5,12) respectively. Find the
vectors $\mathbf{u} = \overrightarrow{OA}$, $\mathbf{v} = \overrightarrow{OB}$ and $\mathbf{w} = \overrightarrow{AB}$
where O is the origin. M is the midpoint
of AB , express \overrightarrow{AM} in terms of \mathbf{u} , \mathbf{v}
and \mathbf{w} and find the length $|AM|$.

Where does the tangent to $y = \sin(x)$
at the point where $x = \frac{\pi}{6}$ cross the
coordinate axes.

Find the binomial expansion of
 $y = \frac{(2x+3)^{\frac{1}{2}}}{3+4x}$ and state the values of
 x for which this expansion converges.

An arithmetic series has second term 9
and eighth term 51. Find the sum of the
first 20 terms.

Find the stationary points of
 $y = \frac{3x^2 + 7x + 3}{e^x}$

l_1 is a line with gradient 2 passing
through the point (5,2). C_1 is a circle,
centre (4,2) with radius 5. Find where l_1
and C_1 intersect.

Find the derivative of $y = x^3 + 3x^2$
from first principles.

Prove
 $\sec^2(x) + \operatorname{cosec}^2(x) = \sec^2(x)\operatorname{cosec}^2(x)$

$(x-2)$ and $(x+3)$ are both factors of
 $p(x) = x^4 + ax^3 + bx^2 - 15x + 18$.
Find a and b and hence find all roots of
 $p(x)$.