

Question 1

Find

$$\sum_{r=1}^n (2r + 1)(r^2 + 3r)$$

in the form $\frac{1}{6}n(n + 1)(an^2 + bn + c)$.Pass on the value of a to Question 2.**Question 3**Let $f(x) = x^3 + 3x^2 - bx + 4$ where b is the value from Question 2.Use the Newton-Raphson process twice with initial guess $x_0 = 0$ to obtain an approximate value for one of the roots.Let c be the digit with place value hundredths. Pass this on to Question 4.**Question 5**Prove that $8^n - 1$ is divisible by d , where d is the value from Question 4.Pass on $e = d^2$ to Question 6.**Question 7**Let A be a matrix such that its determinant is the value f from Question 6.Given that $A = \begin{pmatrix} 2 & 1 \\ g & 8 \end{pmatrix}$ find g and pass this on to Question 8.**Question 9**Where x and y are from Question 8, find

$$\sum_{r=x}^y r^2 + 2^r$$

Let your answer be k and pass this value on to Question 10.**Question 11**Three vertices of a square are $(0,0)$, $(2,0)$ and $(0,2)$.An enlargement by scale factor l (where l is the value from question 10) is represented by the matrix S and a rotation of 180° about $(0,0)$ is represented by the matrix T . Find the absolute value of the y -coordinate of the transformed point when you apply S followed by T to the vertex of the square that is opposite the origin. Pass this on to Question 12.

<p style="text-align: center;"><u>Question 2</u></p> <p>Using a from Question 1. Let $z = a + 2i$. Calculate $z^2 z^*$. Let b be the real part of $z^2 z^*$ divided by 3. Pass on b to Question 3</p>	<p style="text-align: center;"><u>Question 4</u></p> <p>A parabola has parametric equations $x = ct^2, y = 2ct$ where c is the value from Question 3. Find the focus, S, and directrix of this parabola. A point P on this parabola has x-coordinate 4. Find the distance $d = PS$ and pass this on to Question 5.</p>
<p style="text-align: center;"><u>Question 6</u></p> <p>Let e be the number from Question 5. Simplify</p> $\frac{9 + ei}{4 + 3i}$ <p>Let f be the square root of the numerator of the imaginary part of your answer. Pass this on to Question 7.</p>	<p style="text-align: center;"><u>Question 8</u></p> <p>With g being the value obtained from Question 7, solve, using a matrix method, the simultaneous equations</p> $\begin{aligned} gx + 2y &= 24 \\ 5x + gy &= 38 \end{aligned}$ <p>Pass your solutions on to Question 9.</p>
<p style="text-align: center;"><u>Question 10</u></p> <p>Show that $(x - 1)$ is a factor of $x^3 - 5x^2 + 193x - k$. Find the other roots of $x^3 - 5x^2 + 193x - k = 0$. Let l be the real part of the other two roots and pass this on to Question 11.</p>	<p style="text-align: center;"><u>Question 12</u></p> <p>A rectangular hyperbola has equation $xy = m$ where m is the number from Question 11. Find an equation for the tangent at the point $P\left(mt, \frac{m}{t}\right)$. What is the area of the triangle formed by the x-axis, y-axis and this tangent?</p>