## **A-Level Christmas Calculated Colouring 2021**



Answer	3	4	1	12	25 / 2	36	8	10
Colour	Brown	Yellow	Grey	Blue	Red	Green	Light Green	Orange

**1)** The absolute value of the product of the gradients of two lines which are perpendicular.

2) Find *a* such that  $\sqrt{a} = 2\sqrt{2}$ . 3) The power of *z* when you simplify  $\frac{xz^3}{y^3} \times \frac{x^5y^4}{3x^2z^2}$ .

4) The radius of the unit circle.

**5)** The x- coordinate of the centre of the circle

 $x^2 - 8x + y^2 + 10y + 16 = 0.$ 

6) The *x*-coordinate of the turning point of  $y = x^2 - 6x + 21$ . 7) Find *b* such that  $(x - 2)(x + b)^2 = x^3 + 6x^2 - 32$ .

8) The remainder on dividing  $x^3 + 4x^2 + 3x + 4$  by (x + 1).

9) The gradient of the line perpendicular to  $y = -\frac{1}{4}x + 3$ . **10)** Given that (x + 5) and (x - 1) are factors of the polynomial  $x^{4} + ax^{3} - 15x^{2} - 19x + b$ , find a. **11)** The gradient of the line passing through (-2, -1) and (0,5). 12) One guarter of the discriminant of the quadratic  $y = 2x^2 + 8x + 3$ . 13) The radius of the circle  $x^{2} + (y - 3)^{2} = 100.$ 14) The denominator when you rationalise —  $^{\prime}10$ **15)** The coefficient of  $x^2$  in the expansion of  $(1 + 3x)^n$  is 252. Find *n* **16)** The y-coordinate of the turning point of  $y = x^2 - 6x + 21$ .

**17)** The largest root (in absolute value) of the equation  $3x^2 - 42x + 72 = 0$ . **18)** 7776 $\frac{2}{5}$ . **19)** Find *y* such that 2x + 4y = 56and x + y = 20. **20)** The denominator of  $\frac{1}{\sqrt{8}}$  when rationalised. **21)**  $20736^{\frac{1}{4}}$ . 22)  $2 \times \begin{pmatrix} 6 \\ 2 \end{pmatrix} + \begin{pmatrix} 4 \\ 2 \end{pmatrix}$  where  $\begin{pmatrix} a \\ b \end{pmatrix}$ represents a choose b. 23) The area of the triangle sandwiched between the x and y-axes and the line which passes through (-2,9) and (6, -3).**24)** Find *x* such that 2x + 4y = 56and x + y = 20.

**25)** Find *n* such that the coefficient of  $x^3$  in the expansion of  $(1 + 3x)^n$  is 540.

**26)** The number of intersection points of the graphs for  $x^2 + y^2 = 9$  and the equation y = 2x + 1 **27)** The gradient of the line which is perpendicular to y = -x + 3. **28)** The square of the radius for the circle  $x^2 + 4x + y^2 - 8y - 5 = 0$ . **29)**  $\sqrt{625}$ 

**30)** The *x*-intercept of the straight pin -x - 4y = -1.

**31)** Find the coefficient of  $x^3$  in the expansion of  $(2 + 3x)^4$  and then divide it by 18.

**32)** The power of *x* when you simplify  $\frac{xz^3}{y^3} \times \frac{x^5y^4}{3x^2z^2}.$ 

 $y^3$   $3x^2z^2$ **33)** Bonus guestion....

**34)** The point (x, x + 1),  $x \in \mathbb{Z}^+$  lies on the circle

 $x^2 - 10x + y^2 - 10y + 25 = 0$ . Find

the *y*-coordinate for the largest x and then multiply by 4.

**35)** The highest common factor of 252 and 180

**36)** Given that (x + 5) and (x - 1) are factors of the polynomial  $p(x) = x^4 + ax^3 - 15x^2 - 19x + b$ , find *b* and add 6.

**37)** The solution of  $2^x = 4^5$ . 38) The length of the line segment between (-5, -1) and (3,5). 39) The radius squared of the circle  $x^2 - 8x + y^2 + 10y + 16 = 0.$ 40) The power of 11 in the prime factor decomposition of 1980. **41**)  $\sqrt{1296}$ **42)** The y-intercept of the line parallel to -2x + y = 12 which passes through (-4,4). **43)** Find a such that  $\sqrt{63} = a\sqrt{7}$ . **44)** Find k such that the point (7.6)lies on the circle  $(x-k)^2 + (y-k)^2 = 25.$ 

**45)** The intersection point of the line x + ay = 34 and y = x + 6 is (4,10). Find *a*. **46)** The repeated root of the polynomial  $P(x) = x^3 - 12x^2 + 45x - 54$ . **47)** The coefficient when you differentiate  $y = 4x^3$ . **48)** One twentieth of the coefficient of *x* when you expand, by the binomial theorem,  $(2 + 3x)^5$ **49)** The points A(-4, -3) and B(4,3) is the diameter of a circle. Find the radius squared of this circle.

**50)** The *y*-intercept of the straight line 25x + 6y = 150