## **A-Level Further Maths Calculated Colouring Christmas 2019**



6	3	25	100	18	4
Green	Yellow	Red	Pink	Blue	Orange

- 1) The imaginary part of 3 + 6i.
- 2) Consider the linear transformation x' = 6x + 18y, y' = 3x + 4y. Represent this transformation by the matrix *A*, what is the entry  $A_{1,1}$ ?
- 3) The real part of the complex solutions of  $x^3 12x^2 + 61x 150 = 0$ .
- 4) One quarter of the imaginary part of (2 + 3i)(4 + 6i).
- 5) The imaginary part of  $\frac{1+2i}{\frac{1}{12}(1+i)}$ .
- 6) The *x* solution of the linear system  $\begin{pmatrix}
  2 & 3 \\
  4 & 1
  \end{pmatrix}
  \begin{pmatrix}
  x \\
  y
  \end{pmatrix} = 
  \begin{pmatrix}
  24 \\
  18
  \end{pmatrix}.$
- 7) Find the denominator of the argument (in radians) of the complex number  $\frac{1}{2} + i\frac{\sqrt{3}}{2}$ .
- 8) Let z = a + 2i. Find The real part of the solution to the equation  $z^3 = -9 + 46i$  (where the real and imaginary parts of *z* are both integers).
- 9) b when you express  $\operatorname{arcosh}(2)$  in the form  $\ln\left(a+\sqrt{b}\right)$ .
- 10) The real part of the number z such that

 $z^2 = -27 + 36i$  where z lies in the positive quadrant.

- 11) The scale factor of the transformation represented by  $\begin{pmatrix} 25 & 0 \\ 0 & 25 \end{pmatrix}$ .
- 12) The square of the magnitude of the complex number

3 + 4i.

- 13) The square of the positive *x*-coordinate where the ellipse  $4x^2 + 10y^2 = 100$  crosses the *x*-axis.
- 14) Square the denominator obtained when you evaluate sech  $(\ln(3))$ .
- 15) The absolute value of the imaginary part of the solutions to the equation  $z^2 200z + 10625$ .
- 16) Express the ellipse  $\frac{x^2}{25} + \frac{y^2}{10} = 1$  in the form  $ax^2 + by^2 = c$  where a and b are integers in the

 $ax^2 + by^2 = c$  where *a* and *b* are integers in their simplest form. Double *c*.

- 17) The radius of the locus satisfying |z (3 + 2i)| = 100.
- 18) Consider a mass oscillating on a spring. It is proposed that the frequency can be modelled as  $f = pk^{\alpha}m^{\beta}x^{\gamma}$  where *p* is a constant, *k* is the spring constant in kgs<sup>-2</sup>, *m* is the mass and *x* is the maximum extension of the spring in metres. Find  $\alpha$  and multiply it by 200.
- 19) The vertical asymptotes of  $\frac{x^2 + 3x + 1}{x^2 104x + 400}$  are

x = a and x = b where b > a. Find b.

20) Let 
$$z = 8 + \sqrt{36i}$$
, find  $zz^*$ .

- 21) The determinant of  $\begin{pmatrix} 4 & -1 \\ 2 & 4 \end{pmatrix}$ .
- 22) The bottom entry of the right hand side when you write the simultaneous equations 2x + 3y = 24 and 4x + y = 18 in matrix form.

The real part of  $\frac{1+2i}{\frac{1}{12}(1+i)}$ . 23) Given that  $\sinh(x) = \frac{3}{4}$ , find  $\sinh(2x)$  and multiply the 24) denominator by 2. The imaginary part of (3 + 2i) + (4 + 20i) - (3 + 4i). 25) *n* such that  $(1 + 3i)^n = 28 - 96i$ . 26) The absolute value of the imaginary part of the 27) complex solutions of  $x^3 - 12x^2 + 61x - 150 = 0$ . The real part of (3 + 2i) + (4 + 20i) - (3 + 4i). 28) 29) If the transformation represented by the matrix  $\begin{pmatrix} 5 & 0 \\ 0 & 5 \end{pmatrix}$  is applied to a shape, by what factor does the area of that shape increase. Find the cartesian equation of the locus 30) |z-2| = |z+6| in the form x = a. The number *a* such that  $\sum_{n=1}^{n} r^2 = \frac{1}{a}n(n+1)(2n+1).$ 31) 40 subtracted from the imaginary part of  $(3 + 2i)^3$ . 32) 33) The *y* solution of the linear system  $\begin{pmatrix} 2 & 3 \\ 4 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 24 \\ 18 \end{pmatrix}.$ The real root of  $p(x) = x^3 - 12x^2 + 61x - 150$ . 34) The imaginary part of the number z such that 35)  $z^2 = -27 + 36i$  where z lies in the positive quadrant. Consider the linear transformation x' = 6x + 18y, 36) y' = 3x + 4y. Represent this transformation by the

matrix A, what is the entry  $A_{21}$ ?

- 37) The denominator of cosech  $(\ln(3))$ .
- 38) Find the equation of the vertical asymptote of the rational function  $y = \frac{x+1}{x-3}$  in the form x = a.
- 39) Find the *y*-coordinate of the point that is mapped to  $\begin{pmatrix} 203\\106 \end{pmatrix}$  by the transformation matrix  $T = \begin{pmatrix} 2 & 1\\1 & 2 \end{pmatrix}$ . 40) Let  $A = \begin{pmatrix} 3 & 1\\11 & 4 \end{pmatrix}^{-1}$ . Find  $A_{2,2}$ .
- 41) The square of the largest eigenvalue of the matrix  $A = \begin{pmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{pmatrix}.$ 42) The value *a* such that  $\frac{25}{-i} = ai.$
- 43) Write the ellipse  $4x^2 + 10y^2 = 100$  in the standard

form 
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$
. What is  $a^2$ ?  
44) Let  $B = \begin{pmatrix} 2 & 1 \\ 4 & 2 \end{pmatrix} \begin{pmatrix} 10 & 1 \\ 5 & 2 \end{pmatrix}$ . Find  $B_{1,1}$ 

- 45) The square of the denominator of the fraction obtained when evaluating  $\cosh(\ln(5))$ .
- 46) The absolute value of the real part of the solutions to the equation  $z^2 200z + 10625$ .
- 47) If an enlargement of scale factor 10 is applied to a shape, then what is the determinant of the matrix representing the transformation?

- 48) Find the x-coordinate of the point that is mapped to  $\binom{203}{106}$  by the transformation matrix  $T = \begin{pmatrix} 2 & 1 \\ 1 & 2 \end{pmatrix}$ .
- Find the determinant of the matrix  $A^2$  where 49)  $A = \begin{pmatrix} 4 & 3 \\ 2 & 4 \end{pmatrix}.$
- The number a where 50)

$$\left[10\left(\cos\left(\frac{\pi}{4}\right) + i\sin\left(\frac{\pi}{4}\right)\right)\right]^2 \text{ is expressed in }$$

the form ai.

- *a* such that  $\begin{pmatrix} 3 & 17 \\ 2 & 5 \end{pmatrix} + \begin{pmatrix} 15 & 2 \\ 1 & 9 \end{pmatrix} = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$ . 51)
- The number *n* such that  $\sum r = 171$ . 52)
- 14 more than the y- coordinate for the maximum 53) point of the rational function  $y = \frac{x^2 + 6x + 9}{x^2 + 3x + 3}$ . Find  $\frac{(2+3i)^2}{1+i}$  in the form  $\frac{p}{q} + \frac{r}{s}i$ . Find r + 1. 54)

- Find the determinant of the matrix  $\begin{pmatrix} -2 & 2 & -3 \\ -1 & 1 & 3 \\ 2 & 0 & -1 \end{pmatrix}$ . 55)
- Find *a* such that  $r^{2}(r+1)^{2} r^{2}(r-1)^{2} = ar^{3}$ . Use 56) this and the method of differences to prove  $\sum^{n} r^{3} = \frac{1}{4}n^{2}(n+1)^{2}.$
- The square of the denominator for *x* such that 57) artanh(x) = ln  $(\sqrt{3})$ . The vertical asymptotes of  $\frac{x^2 + 3x + 1}{x^2 - 104x + 400}$  are
- 58) x = a and x = b where b > a. Find a.
- Use dimensional analysis to find the dimensions of the 59) spring constant k in Hooke's Law, T = kx (T is tension, x is extension). Multiply the absolute value of the non-unity power in the dimensional expression by two.
- Consider the linear transformation x' = 6x + 18y, 60) y' = 3x + 4y. Represent this transformation by the matrix A, what is the entry  $A_{2,2}$ ?